

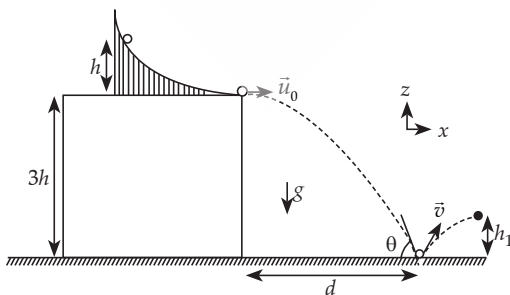
## Physics

**General Instructions:**

**SECTION 1 (Maximum Marks: 12)**

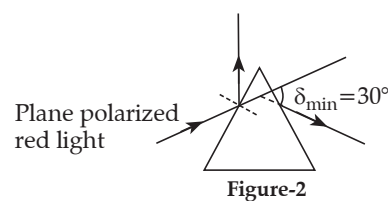
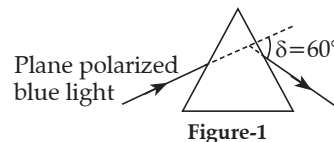
- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:
  - Full Marks* : +4 **ONLY** if (all) the correct option(s) is(are) chosen;
  - Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen;
  - Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;
  - Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;
  - Zero Mark* : 0 If none of the options is chosen (i.e. the question is unanswered);
  - Negative Marks* : -2 In all other cases.
- For example, in a question, if (A), (B) and (D) are the **ONLY** three options corresponding to correct answers, then choosing **ONLY** (A), (B) and (D) will get +4 marks; choosing **ONLY** (A) and (B) will get +2 marks; choosing **ONLY** (A) and (D) will get +2 marks; choosing **ONLY** (B) and (D) will get +2 marks; choosing **ONLY** (A) will get +1 mark; choosing **ONLY** (B) will get +1 mark; choosing **ONLY** (D) will get +1 mark; choosing no option (i.e. the question is unanswered) will get 0 marks; and choosing any other combination of options will get -2 marks.

- Q. 1.** A slide with a frictionless curved surface, which becomes horizontal at its lower end, is fixed on the terrace of a building of height  $3h$  from the ground, as shown in the figure. A spherical ball of mass  $m$  is released on the slide from rest at a height  $h$  from the top of the terrace. The ball leaves the slide with a velocity  $\vec{u}_0 = u_0 \hat{x}$  and falls on the ground at a distance  $d$  from the building making an angle  $\theta$  with the horizontal. It bounces off with a velocity  $\vec{v}$  and reaches a maximum height  $h_1$ . The acceleration due to gravity is  $g$  and the coefficient of restitution of the ground is  $1/\sqrt{3}$ . Which of the following statement(s) is(are) correct?



- (A)  $\vec{u}_0 = \sqrt{2gh} \hat{x}$       (B)  $\vec{v} = \sqrt{2gh} (\hat{x} - \hat{z})$   
 (C)  $\theta = 60^\circ$       (D)  $d/h_1 = 2\sqrt{3}$

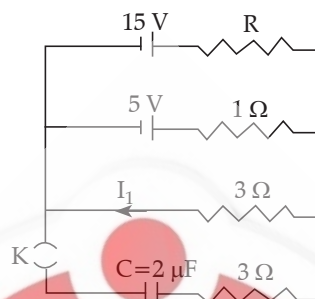
- Q. 2.** A plane polarized blue light ray is incident on a prism such that there is no reflection from the surface of the prism. The angle of deviation of the emergent ray is  $\delta = 60^\circ$  (see Figure-1). The angle of minimum deviation for red light from the same prism is  $\delta_{\min} = 30^\circ$  (see Figure-2). The refractive index of the prism material for blue light is  $\sqrt{3}$ . Which of the following statement(s) is(are) correct?



- (A) The blue light is polarized in the plane of incidence.
- (B) The angle of the prism is  $45^\circ$ .
- (C) The refractive index of the material of the prism for red light is  $\sqrt{2}$ .
- (D) The angle of refraction for blue light in air at the exit plane of the prism is  $60^\circ$ .

Q. 3. In a circuit shown in the figure, the capacitor C is initially uncharged and the key K is open. In this condition, a current of 1 A flows through the  $1\ \Omega$  resistor. The key is closed at time  $t = t_0$ . Which of the following statement(s) is(are) correct?

[Given:  $e^{-1} = 0.36$ ]



- (A) The value of the resistance R is  $3\ \Omega$ .
- (B) For  $t < t_0$ , the value of current  $I_1$  is 2 A.
- (C) At  $t = t_0 + 7.2\ \mu\text{s}$ , the current in the capacitor is 0.6 A.
- (D) For  $t \rightarrow \infty$ , the charge on the capacitor is  $12\ \mu\text{C}$ .

**General Instructions:**

**SECTION 2 (Maximum Marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +3 If **ONLY** the correct option is chosen;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

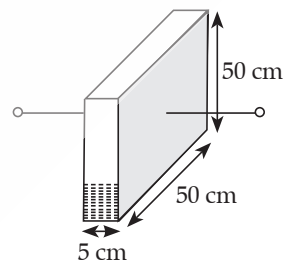
Negative Marks : -1 In all other cases.

Q. 4. A bar of mass  $M = 1.00\ \text{kg}$  and length  $L = 0.20\ \text{m}$  is lying on a horizontal frictionless surface. One end of the bar is pivoted at a point about which it is free to rotate. A small mass  $m = 0.10\ \text{kg}$  is moving on the same horizontal surface with  $5.00\ \text{m s}^{-1}$  speed on a path perpendicular to the bar. It hits the bar at a distance  $L/2$  from the pivoted end and returns back on the same path with speed  $v$ . After this elastic collision, the bar rotates with an angular velocity  $\omega$ . Which of the following statement is correct?

- (A)  $\omega = 6.98\ \text{rad s}^{-1}$  and  $v = 4.30\ \text{m s}^{-1}$
- (B)  $\omega = 3.75\ \text{rad s}^{-1}$  and  $v = 4.30\ \text{m s}^{-1}$
- (C)  $\omega = 3.75\ \text{rad s}^{-1}$  and  $v = 10.0\ \text{m s}^{-1}$
- (D)  $\omega = 6.80\ \text{rad s}^{-1}$  and  $v = 4.10\ \text{m s}^{-1}$

Q. 5. A container has a base of  $50\ \text{cm} \times 50\ \text{cm}$  and height  $50\ \text{cm}$ , as shown in the figure. It has two parallel electrically conducting walls each of area  $50\ \text{cm} \times 50\ \text{cm}$ . The remaining walls of the container are thin and non-conducting. The container is being filled with a liquid of dielectric constant 3 at a uniform rate of  $250\ \text{cm}^3\ \text{s}^{-1}$ . What is the value of the capacitance of the container after 10 seconds?

[Given: Permittivity of free space  $\epsilon_0 = 9 \times 10^{-12}\ \text{C}^2\ \text{N}^{-1}\ \text{m}^{-2}$ , the effects of the non-conducting walls on the capacitance are negligible]



- (A) 27 pF
- (B) 63 pF
- (C) 81 pF
- (D) 135 pF

Q. 6. One mole of an ideal gas expands adiabatically from an initial state  $(T_A, V_0)$  to final state  $(T_f, 5V_0)$ . Another mole of the same gas expands isothermally from a different initial state  $(T_B, V_0)$  to the same final state  $(T_f, 5V_0)$ . The ratio of the specific heats at constant pressure and constant volume of this ideal gas is  $\gamma$ . What is the ratio  $T_A/T_B$ ?

- (A)  $5^{\gamma-1}$
- (B)  $5^{1-\gamma}$
- (C)  $5^\gamma$
- (D)  $5^{1+\gamma}$

Q. 7. Two satellites P and Q are moving in different circular orbits around the Earth (radius R). The heights of P and Q from the Earth surface are  $h_P$  and  $h_Q$ , respectively, where  $h_P = R/3$ . The accelerations of P and Q due to Earth's gravity are  $g_P$  and  $g_Q$ , respectively. If  $g_P/g_Q = 36/25$ , what is the value of  $h_Q$ ?

- (A)  $3R/5$
- (B)  $R/6$
- (C)  $6R/5$
- (D)  $5R/6$

**General Instructions:****SECTION 3 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:

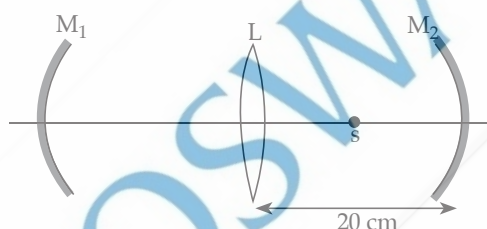
Full Marks : +4 If **ONLY** the correct integer is entered;

Zero Marks : 0 In all other cases.

**Q. 8.** A Hydrogen-like atom has atomic number  $Z$ . Photons emitted in the electronic transitions from level  $n = 4$  to level  $n = 3$  in these atoms are used to perform photoelectric effect experiment on a target metal. The maximum kinetic energy of the photoelectrons generated is  $1.95 \text{ eV}$ . If the photoelectric threshold wavelength for the target metal is  $310 \text{ nm}$ , the value of  $Z$  is \_\_\_\_\_.

[Given:  $hc = 1240 \text{ eV}\cdot\text{nm}$  and  $Rhc = 13.6 \text{ eV}$ , where  $R$  is the Rydberg constant,  $h$  is the Planck's constant and  $c$  is the speed of light in vacuum]

**Q. 9.** An optical arrangement consists of two concave mirrors  $M_1$  and  $M_2$ , and a convex lens  $L$  with a common principal axis, as shown in the figure. The focal length of  $L$  is  $10 \text{ cm}$ . The radii of curvature of  $M_1$  and  $M_2$  are  $20 \text{ cm}$  and  $24 \text{ cm}$ , respectively. The distance between  $L$  and  $M_2$  is  $20 \text{ cm}$ . A point object  $S$  is placed at the mid-point between  $L$  and  $M_2$  on the axis. When the distance between  $L$  and  $M_1$  is  $n/7 \text{ cm}$ , one of the images coincides with  $S$ . The value of  $n$  is \_\_\_\_\_.

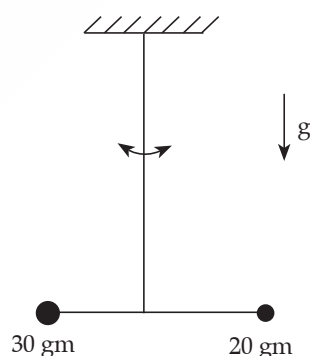


**Q. 10.** In an experiment for determination of the focal length of a thin convex lens, the distance of the object from the lens is  $10 \pm 0.1 \text{ cm}$  and the distance of its real image from the lens is  $20 \pm 0.2 \text{ cm}$ . The error in the determination of focal length of the lens is  $n\%$ . The value of  $n$  is \_\_\_\_\_.

**Q. 11.** A closed container contains a homogeneous mixture of two moles of an ideal monoatomic gas ( $\gamma = 5/3$ ) and one mole of an ideal diatomic gas ( $\gamma = 7/5$ ). Here,  $\gamma$  is the ratio of the specific heats at constant pressure and constant volume of an ideal gas. The gas mixture does a work of  $66 \text{ Joule}$  when heated at constant pressure. The change in its internal energy is \_\_\_\_\_ Joule.

**Q. 12.** A person of height  $1.6 \text{ m}$  is walking away from a lamp post of height  $4 \text{ m}$  along a straight path on the flat ground. The lamp post and the person are always perpendicular to the ground. If the speed of the person is  $60 \text{ cm s}^{-1}$ , the speed of the tip of the person's shadow on the ground with respect to the person is \_\_\_\_\_  $\text{cm s}^{-1}$ .

**Q. 13.** Two point-like objects of masses  $20 \text{ gm}$  and  $30 \text{ gm}$  are fixed at the two ends of a rigid massless rod of length  $10 \text{ cm}$ . This system is suspended vertically from a rigid ceiling using a thin wire attached to its center of mass, as shown in the figure. The resulting torsional pendulum undergoes small oscillations. The torsional constant of the wire is  $1.2 \times 10^{-8} \text{ N m rad}^{-1}$ . The angular frequency of the oscillations is  $n \times 10^{-3} \text{ rad s}^{-1}$ . The value of  $n$  is \_\_\_\_\_.

**General Instructions:****SECTION 4 (Maximum Marks: 12)**

- This section contains **FOUR (04)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has **TWO** lists: **List-I** and **List-II**.
- List-I** has **Four** entries (P), (Q), (R) and (S) and **List-II** has **Five** entries (1), (2), (3), (4) and (5).
- FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +3 **ONLY** if the option corresponding to the correct combination is chosen;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks : -1 In all other cases.



**Q. 14.** List-I shows different radioactive decay processes and List-II provides possible emitted particles. Match each entry in List-I with an appropriate entry from List-II, and choose the correct option.

- | List-I  | List-II   |
|---|---|
| (P) ${}_{92}^{238}\text{U} \rightarrow {}_{91}^{234}\text{Pa}$  | (1) one $\alpha$ particle and one $\beta^+$ particle    |
| (Q) ${}_{82}^{214}\text{Pb} \rightarrow {}_{82}^{210}\text{Pb}$ | (2) three $\beta^-$ particles and one $\alpha$ particle |
| (R) ${}_{81}^{210}\text{Tl} \rightarrow {}_{82}^{206}\text{Pb}$ | (3) two $\beta^-$ particles and one $\alpha$ particle   |
| (S) ${}_{91}^{228}\text{Pa} \rightarrow {}_{88}^{224}\text{Ra}$ | (4) one $\alpha$ particle and one $\beta^-$ particle    |
|   | (5) one $\alpha$ particle and two $\beta^+$ particles   |

- (A) P  $\rightarrow$  4, Q  $\rightarrow$  3, R  $\rightarrow$  2, S  $\rightarrow$  1  
 (B) P  $\rightarrow$  4, Q  $\rightarrow$  1, R  $\rightarrow$  2, S  $\rightarrow$  5  
 (C) P  $\rightarrow$  5, Q  $\rightarrow$  3, R  $\rightarrow$  1, S  $\rightarrow$  4  
 (D) P  $\rightarrow$  5, Q  $\rightarrow$  1, R  $\rightarrow$  3, S  $\rightarrow$  2

**Q. 15.** Match the temperature of a black body given in List-I with an appropriate statement in List-II, and choose the correct option.

[Given: Wien's constant as  $2.9 \times 10^{-3}$  m-K and  $\frac{hc}{e} = 1.24 \times 10^{-6}$  V-m]

- | List-I      | List-II   |
|-------------|---|
| (P) 2000 K  | (1) The radiation at peak wavelength can lead to emission of photoelectrons from a metal of work function 4 eV.       |
| (Q) 3000 K  | (2) The radiation at peak wavelength is visible to human eye.   |
| (R) 5000 K  | (3) The radiation at peak emission wavelength will result in the widest central maximum of a single slit diffraction. |
| (S) 10000 K | (4) The power emitted per unit area is 1/16 of that emitted by a blackbody at temperature 6000 K.                     |
|             | (5) The radiation at peak emission wavelength can be used to image human bones.                                       |

- (A) P  $\rightarrow$  3, Q  $\rightarrow$  5, R  $\rightarrow$  2, S  $\rightarrow$  3  
 (B) P  $\rightarrow$  3, Q  $\rightarrow$  2, R  $\rightarrow$  4, S  $\rightarrow$  1  
 (C) P  $\rightarrow$  3, Q  $\rightarrow$  4, R  $\rightarrow$  2, S  $\rightarrow$  1  
 (D) P  $\rightarrow$  1, Q  $\rightarrow$  2, R  $\rightarrow$  5, S  $\rightarrow$  3

**Q. 16.** A series LCR circuit is connected to a  $45\sin(\omega t)$  Volt source. The resonant angular frequency of the circuit is  $10^5$  rad  $s^{-1}$  and current amplitude at resonance is  $I_0$ . When the angular frequency of the source is  $\omega = 8 \times 10^4$  rad  $s^{-1}$ , the current amplitude in the circuit is  $0.05 I_0$ . If  $L = 50$  mH, match each entry in List-I with an appropriate value from List-II and choose the correct option.

**List-I**

- (P)  $I_0$  in mA  
 (Q) The quality factor of the circuit  
 (R) The bandwidth of the circuit in rad  $s^{-1}$   
 (S) The peak power dissipated at resonance in Watt

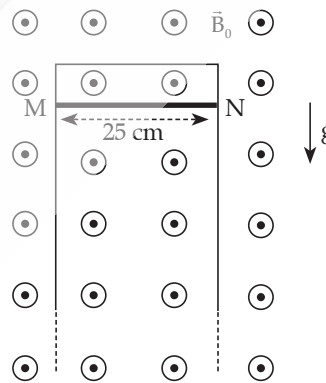
**List-II**

- (1) 44.4  
 (2) 18  
 (3) 400  
 (4) 2250  
 (5) 500

- (A) P  $\rightarrow$  2, Q  $\rightarrow$  3, R  $\rightarrow$  5, S  $\rightarrow$  1  
 (B) P  $\rightarrow$  3, Q  $\rightarrow$  1, R  $\rightarrow$  4, S  $\rightarrow$  2  
 (C) P  $\rightarrow$  4, Q  $\rightarrow$  5, R  $\rightarrow$  3, S  $\rightarrow$  1  
 (D) P  $\rightarrow$  4, Q  $\rightarrow$  2, R  $\rightarrow$  1, S  $\rightarrow$  5

**Q. 17.** A thin conducting rod MN of mass 20 gm, length 25 cm and resistance  $10 \Omega$  is held on frictionless, long, perfectly conducting vertical rails as shown in the figure. There is a uniform magnetic field  $B_0 = 4$  T directed perpendicular to the plane of the rod-rail arrangement. The rod is released from rest at time  $t = 0$  and it moves down along the rails. Assume air drag is negligible. Match each quantity in List-I with an appropriate value from List-II, and choose the correct option.

[Given: The acceleration due to gravity  $g = 10$  m  $s^{-2}$  and  $e^{-1} = 0.4$ ]



**List-I**

- (P) At  $t = 0.2$  s, the magnitude of the induced emf in Volt  
 (Q) At  $t = 0.2$  s, the magnitude of the magnetic force in Newton  
 (R) At  $t = 0.2$  s, the power dissipated as heat in Watt  
 (S) The magnitude of terminal velocity of the rod in m  $s^{-1}$

**List-II**

- (1) 0.07  
 (2) 0.14  
 (3) 1.20  
 (4) 0.12  
 (5) 2.00

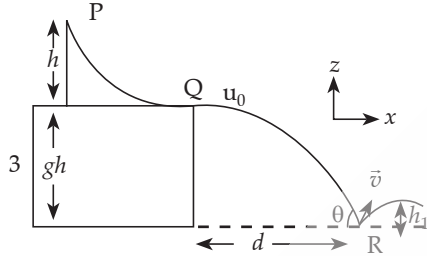
- (A) P  $\rightarrow$  5, Q  $\rightarrow$  2, R  $\rightarrow$  3, S  $\rightarrow$  1  
 (B) P  $\rightarrow$  3, Q  $\rightarrow$  1, R  $\rightarrow$  4, S  $\rightarrow$  5  
 (C) P  $\rightarrow$  4, Q  $\rightarrow$  3, R  $\rightarrow$  1, S  $\rightarrow$  2  
 (D) P  $\rightarrow$  3, Q  $\rightarrow$  4, R  $\rightarrow$  2, S  $\rightarrow$  5

**ANSWER KEY**

Q.No.	Answer key	Topic's name	Chapter's name
<b>Section -I</b>			
1	(A, C, D)	Collision	Center of Mass
2	(A, C, D)	Deviation and Dispersion from Prism	Geometric Optics
3	(A, B, C, D)	Kirchhoff's law and Combination of batteries	Current Electricity
<b>Section -II</b>			
4	(A)	Collision of Point mass with Rigid bodies	System of Particles and Rotational Motion
5	(B)	Polarisation and Dielectric	Electrostatics and Capacitors
6	(A)	Thermodynamic process	Kinematic Theory of Gases and Thermodynamics
7	(A)	Acceleration due to gravity	Gravitation
<b>Section -III</b>			
8	3	Photoelectric Effect	Dual Nature of Matter and Radiation
9	150	Lens and Mirror combination	Geometric Optics
10	1	Refraction through lens	Geometric Optics
11	121	Thermodynamic process	Kinematic Theory of Gases and Thermodynamics
12	40	Miscellaneous	Geometric Optics
13	10	Torsional Pendulum	Simple Harmonic Motion
<b>Section -IV</b>			
14	(A)	Radioactive Decay	Nuclear Physics
15	(C)	Black body Radiation	Thermal Properties of Matter
16	(B)	LCR Circuit	Electromagnetic Effect and Alternating Current
17	(D)	Motional Electromagnetic Effect	Electromagnetic Effect and Alternating Current

## ANSWERS WITH EXPLANATIONS

1. Correct options are (A, C and D).



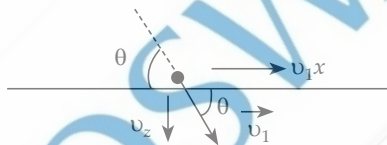
From energy conservation between P and Q

$$\begin{aligned} \downarrow PE &= \uparrow KE \\ mgh &= \frac{1}{2} mu_0^2 \\ \Rightarrow u_0 &= \sqrt{2gh} \\ \vec{u}_0 &= \sqrt{2gh} \hat{x} \end{aligned}$$

(A) is correct.

At R

Before impact



Between P and R

$$\begin{aligned} \downarrow PE &= \uparrow KE \\ mg(4h) &= \frac{1}{2} mv_1^2 \\ v_1 &= \sqrt{8gh} \end{aligned}$$

Also  $v_{1x} = u_0$  [ $\because$  Horizontal velocity doesn't change in projectile motion.]

$$\text{Again } d = u_0 t = u_0 \times \sqrt{\frac{2 \times 3h}{g}} = \sqrt{2gh} \cdot \sqrt{\frac{6h}{g}}$$

$$= \sqrt{12}h = 2\sqrt{3}h$$

$$v_1^2 = v_{1x}^2 + v_{1z}^2$$

$$= u_0^2 + v_{1z}^2$$

$$8gh = 2gh + v_{1z}^2$$

$$\Rightarrow v_{1z} = \sqrt{6gh}$$

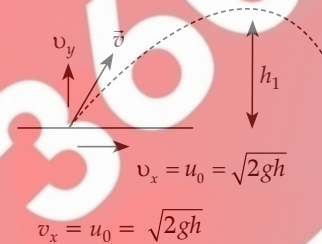
$$\tan \theta = \frac{v_{1z}}{v_{1x}} = \frac{\sqrt{6gh}}{\sqrt{2gh}} = \sqrt{3}$$

$$\Rightarrow \tan \theta = \sqrt{3}$$

$$\Rightarrow \theta = 60^\circ$$

(C) is correct.

After impact



Velocity of separation =  $e \times$  velocity of approach.

$$v_y = e \times v_{1y}$$

$$= \frac{1}{\sqrt{3}} \times \sqrt{6gh} = \sqrt{2gh}$$

$$h_1 = \frac{v_y^2}{2g}$$

$$= \frac{2gh}{2g} = h$$

$$\frac{d}{h} = \frac{2\sqrt{3}h}{h} = 2\sqrt{3}$$

(D) is correct.

$$\begin{aligned} \vec{v}_x &= v_x \hat{x} + v_z \hat{z} \\ &= \sqrt{2gh} (\hat{x} + \hat{z}) \end{aligned}$$

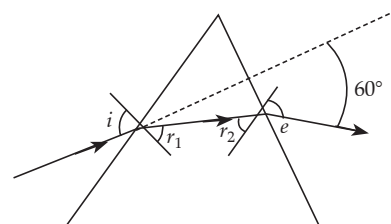
(B) is not correct.

2. Correct options are (A, C and D).

If a light is incident on a surface then for Brewster's angle light is polarised in direction perpendicular to plane of incidence.

$\therefore$  No reflection for blue light is seen.

$\Rightarrow$  It must be polarised in plane of incidence.



$$\tan i = \mu$$

[for incidence at Brewster's angle]

$$\begin{aligned} \tan i &= \sqrt{3} \\ i &= 60^\circ \\ \delta &= i + e - A \\ 60 &= 60 + e - A \\ \Rightarrow A &= e \\ \frac{\sin i}{\sin r_1} &= \sqrt{3} \\ \Rightarrow \frac{\sin 60}{\sin r_1} &= \sqrt{3} \Rightarrow r_1 = 30^\circ \\ r_2 &= A - r_1 \\ \mu \sin(A - r_1) &= \sin e \\ \Rightarrow \sqrt{3} \sin(A - 30) &= \sin A \\ r_3 [\sin A \cos 30^\circ - \cos A \sin 30] &= \sin A \\ \Rightarrow \frac{\sqrt{3}}{2} (\sqrt{3} - \cot A) &= 1 \\ \Rightarrow \cot A &= \sqrt{3} - \frac{2}{\sqrt{3}} = \frac{1}{\sqrt{3}} \\ \Rightarrow \cot A &= \frac{1}{\sqrt{3}} \\ \Rightarrow A &= 60^\circ \\ \text{So, } e &= 60^\circ \text{ (for blue)} \end{aligned}$$

For red,

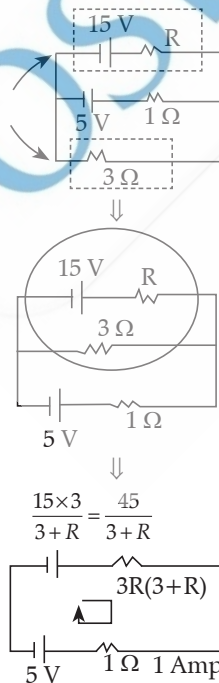
$$\begin{aligned} \mu &= \frac{\sin\left(\frac{\delta_m + A}{2}\right)}{\sin\frac{A}{2}} \\ &= \frac{\sin\left(\frac{30 + 60}{2}\right)}{\sin\frac{60}{2}} = \frac{\sin 45}{\sin 30} = \frac{1/\sqrt{2}}{1/2} \end{aligned}$$

$$\mu_{\text{red}} = \sqrt{2}$$

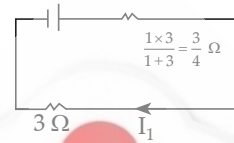
(A), (C), (D) are correct.

3. Correct options are (A, B, C and D).

At  $t < t_0$



$$\frac{15 \times 1 + 5 \times R}{1 + R} = \frac{15}{2} \text{ V}$$



At  $t < t_0$

$$i = \frac{\left(\frac{45}{3+R}\right) - 5}{1} = \frac{3R}{3+R}$$

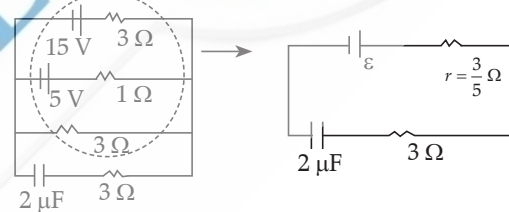
$$1 = \frac{45 - 15 - 5R}{3 + 4R}$$

$\Rightarrow R = 3 \Omega$   
(A) is correct.

$$I_1 = \frac{15}{3 + \frac{3}{4}} \Rightarrow I_1 = 2 \text{ A}$$

(B) is correct.

At  $t > t_0$



$$\frac{\epsilon}{r} = \frac{15}{3} + \frac{5}{1} + \frac{0}{3}$$

$$\frac{1}{r} = \frac{1}{3} + \frac{1}{1} + \frac{1}{3} = \frac{5}{3}$$

$$\epsilon = 10 \times \frac{3}{5} \Rightarrow 6 \text{ V}$$

At  $t \rightarrow \infty$

$$q = C\epsilon = 2 \times 10^{-6} \times 6 = 12 \mu\text{C}$$

Time constant  $\tau = RC$

$$= (r + 3) 2 \mu\text{C}$$

$$= \left(\frac{3}{5} + 3\right) \times 12 = 7.2 \mu\text{s}$$

$$i = i_0 e^{-t/\tau}$$

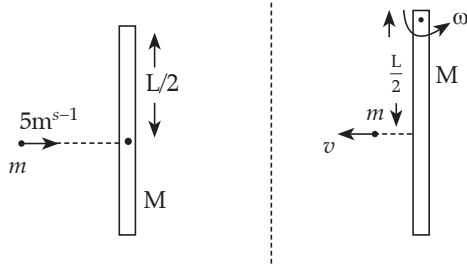
$$i_0 = \frac{\epsilon}{r + 3} = \frac{6}{\left(3 + \frac{3}{5}\right)}$$

$$\Rightarrow i = \frac{6}{18} \times e^{-7.2/1.2}$$

$$= \frac{5}{3} \times 0.36 = 0.6 \text{ A}$$

All options are correct.

4. Correct option is (A).



About hinge  $\rightarrow$  angular momentum is conserved.

$$L_{\text{before}} = L_{\text{after}}$$

$$mv_0 \frac{L}{2} = I\omega - mv \frac{L}{2}$$

$$\Rightarrow 0.1 \times 5 \times \frac{0.2}{2} = \frac{1}{3} \times 1 \times 0.2^2 \omega - 0.1 \times v \times \frac{0.2}{2}$$

$$\Rightarrow \frac{4\omega}{3} = 5 + v \quad \dots(1)$$

For Elastic collision

At point of impact,  
velocity of separation = velocity of approach

$$\frac{\omega L}{2} - (-v) = 5$$

$$\Rightarrow \frac{\omega \times 0.2}{2} + v = 5$$

$$\frac{\omega}{10} = 5 - v \quad \dots(2)$$

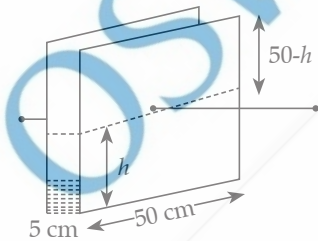
From (1) and (2),

$$\omega = \frac{300}{43} \text{ rad sec}^{-1}$$

$$\Rightarrow \omega = 6.976 \text{ rad sec}^{-1}$$

$$\text{and } v = 4.3 \text{ m sec}^{-1}$$

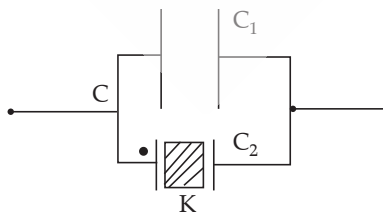
5. Correct option is (B).



$$\text{Volume of dielectric filled in 10 sec} \\ = 250 \times 10 = 2500 \text{ cm}^3$$

$$h \times 50 \times 5 = 2500$$

$$\Rightarrow h = 10 \text{ cm}$$



$$C_1 = \frac{\epsilon_0 A_1}{d}, C_2 = \frac{\epsilon_0 A_2}{d} K$$

$$A_1 = 50 \times (50 - h)$$

$$A_2 = 50 \times h$$

$$C_{\text{eq}} = C_1 + C_2$$

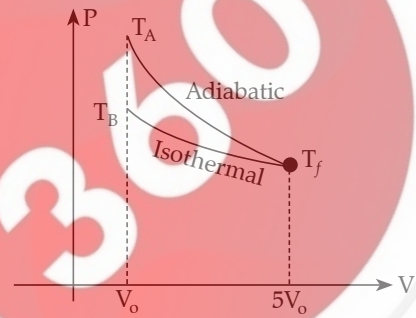
$$= \frac{\epsilon_0 50(50 - h) \text{ cm}^2}{5 \text{ cm}} + \frac{3 \times \epsilon_0 \times 50 \times h}{5 \text{ cm}}$$

$$= \epsilon_0 \left[ \frac{50 \times 40}{5} + \frac{3 \times 50 \times 10}{5} \right] \times 10^{-2}$$

$$= 7\epsilon_0 = 63 \times 10^{-12}$$

$$= 63 \text{ pF}$$

6. Correct option is (A).



$$T_B = T_f \quad [\because \text{process is isothermal}]$$

$$T_A V_0^{\gamma-1} = T_f (5V_0)^{\gamma-1} \quad [\because \text{process is adiabatic}]$$

$$T_A = T_f 5^{\gamma-1}$$

$$= T_B 5^{\gamma-1}$$

$$\Rightarrow \frac{T_A}{T_B} = 5^{\gamma-1}$$

7. Correct option is (A).

Above the surface of earth

$$g = \frac{g_0}{\left(1 + \frac{h}{R}\right)^2}$$

$$\frac{g_P}{g_Q} = \frac{g_0}{\left(1 + \frac{h_P}{R}\right)^2} \times \frac{\left(1 + \frac{h_Q}{R}\right)^2}{g_0}$$

$$\Rightarrow \frac{36}{25} = \frac{\left(1 + \frac{h_Q}{R}\right)^2}{\left(1 + \frac{h_P}{R}\right)^2}$$

$$\Rightarrow \frac{6}{5} = \frac{\left(1 + \frac{h_Q}{R}\right)}{\left(1 + \frac{R/3}{R}\right)}$$

$$\Rightarrow \frac{h_Q}{R} + 1 = \frac{6}{5} \times \frac{4}{3}$$

$$= \frac{8}{5}$$

$$\boxed{h_Q = \frac{3}{5} R}$$



8. Correct answer is [3].

Energy of photon (E)

$$E = 13.6Z^2 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

$$= 13.6Z^2 \left( \frac{1}{3^2} - \frac{1}{4^2} \right)$$

$$= \frac{13.6 \times 7 \times Z^2}{16 \times 9}$$

During photo electric effect

$$KE_{\max} = E - \phi, \quad \phi = \frac{hc}{\lambda_0} = \frac{1240}{310} = 4\text{eV}$$

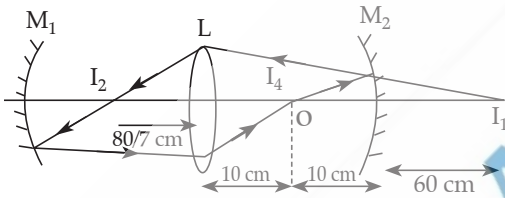
$$\Rightarrow 1.95 = \frac{13.6 \times 7 \times Z^2}{16 \times 9} - 4$$

$$13.6 \times 7 \times Z^2 = 9 \times 95.2$$

$$Z^2 = 9$$

$$\Rightarrow Z = 3$$

9. Correct answer is [150].



For Image I<sub>1</sub>

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{v} + \frac{1}{-10} = \frac{1}{-12}$$

$$\frac{1}{v} = \frac{1}{10} - \frac{1}{12}$$

$$\Rightarrow v = 60\text{ cm}$$

For Image I<sub>2</sub>,

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{-80} = \frac{1}{10}$$

$$\Rightarrow v = \frac{80}{7}\text{ cm}$$

For Image I<sub>3</sub>

Image I<sub>3</sub> must be such that I<sub>4</sub> is formed at O and O is at focus of L, so I<sub>3</sub> must be at infinity.

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{\infty} + \frac{1}{u} = \frac{1}{-10}$$

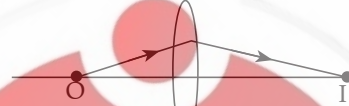
$$\Rightarrow u = -10\text{ cm}$$

Separation between L and M,

$$10 + \frac{80}{7} = \frac{150}{7}$$

$$\Rightarrow n = 150$$

10. Correct answer is [1].



$$u = -10\text{ cm}$$

$$\Delta u = 0.1\text{ cm}$$

$$v = +20\text{ cm}$$

$$\Delta v = 0.2\text{ cm}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{+20} - \frac{1}{-10} = \frac{1}{f}$$

$$f = \frac{20}{3}\text{ cm}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{dv}{v^2} - \frac{du}{u^2} = \frac{df}{f^2}$$

$\Rightarrow$

Error

$$\frac{\Delta v}{v^2} + \frac{\Delta u}{u^2} = \frac{\Delta f}{f} \left( \frac{1}{f} \right)$$

$$\frac{0.2}{20^2} + \frac{0.1}{10^2} = \frac{\Delta f}{f} \times \frac{3}{20}$$

$$\frac{\Delta f}{f} = \frac{1}{100}$$

$$\Rightarrow \frac{\Delta f}{f} \times 100 = n$$

$$\Rightarrow n = 1$$

11. Correct answer is [121].

$$\Delta U = nLV \Delta T$$

$$\Delta W = nR \Delta T \quad [\text{at constant pressure}]$$

$$\Rightarrow 66 = nR \Delta T$$

$$\text{Also } (n_1 + n_2)C_V = n_1C_{V1} + n_2C_{V2}$$

$$= 2 \times \frac{R}{\gamma_1 - 1} + 1 \times \frac{R}{\gamma_2 - 1}$$

$$(2 + 1)C_V = 2 \times \frac{3}{2}R + 1 \times \frac{5R}{2}$$

$$\Rightarrow C_V = \frac{11}{6}R$$

$$\Delta U = \frac{11}{6}nR \Delta T$$

$$\Rightarrow \Delta U = \frac{11}{6} \times 60 = 121\text{ J}$$

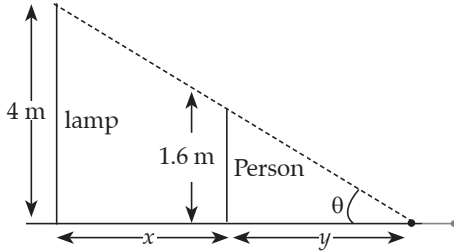
12. Correct answer is [40].

$y$  = distance of tip of shadow from person.

$$\tan \theta = \frac{4}{x+y} = \frac{1.6}{y}$$

$$\Rightarrow 2x = 3y$$

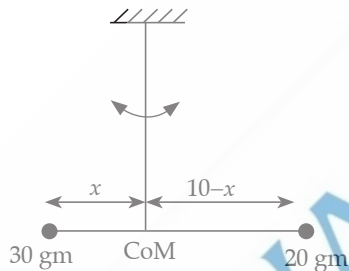
$$2 \frac{dx}{dt} = 3 \frac{dy}{dt}$$



$$\Rightarrow 2 \times 60 = 3 \times \frac{dy}{dt}$$

$$\Rightarrow \frac{dy}{dt} = 40 \text{ cm s}^{-1}$$

13. Correct answer is [10].



Moment of inertia about CoM

$$I = 30 \times x^2 + 20 \times (10-x)^2$$

$$= (30 \times 4^2 + 20 \times 6^2) \times 10^{-3} \times (10^{-2})^2$$

$$= 1.2 \times 10^{-4} \text{ kg m}^2$$

$$\tau = I \alpha$$

$$-K\theta = I\alpha$$

$$\Rightarrow \alpha = \frac{-K}{I} \theta = -\omega^2 \theta$$

$$\Rightarrow \omega^2 = \frac{1.2 \times 10^{-8}}{1.2 \times 10^{-4}}$$

$$\omega^2 = 10^{-4}$$

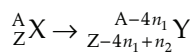
$$\omega = 10^{-2} \text{ rad/s}$$

$$\omega = n \times 10^{-3}$$

$$\boxed{n=10}$$

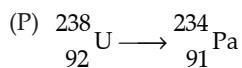
$\Rightarrow$

14. Correct answer is [A].



$n_1$  = no. of  $\alpha$  decay

$n_2$  = no. of  $\beta$  decay

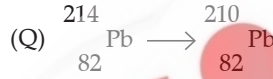


$$238 - 4n_1 = 234 \Rightarrow n_1 = 1$$

$$92 - 2n_1 + n_2 = 91$$

$$\Rightarrow 2n_1 - n_2 = 1 \Rightarrow n_2 = 1$$

$\Rightarrow 1 \alpha$  and  $1 \beta^-$  decay



$$214 - 4n_1 = 210$$

$$\Rightarrow n_1 = 1$$

$$82 - 2n_1 + n_2 = 82$$

$$2n_1 = n_2$$

$$n_2 = 2$$

$1 \alpha$  and  $2 \beta^-$  decay



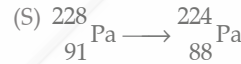
$$210 - 4n_1 = 206$$

$$\Rightarrow n_1 = 1$$

$$81 - 2n_1 + n_2 = 82$$

$$\Rightarrow n_2 = 3$$

$1 \alpha$  and  $3 \beta^-$  decay



$$228 - 4n_1 = 224$$

$$\Rightarrow n_1 = 1$$

$$91 - 2n_1 + n_2 = 88$$

$$n_2 = -1$$

$\Rightarrow \beta^+$  decay occurs

$1 \alpha$  and  $1 \beta^+$  decay



$P \rightarrow 4, Q \rightarrow 3, R \rightarrow 2, S \rightarrow 1.$

15. Correct option is (C).

$$\lambda_0 T = b$$

(P)  $\lambda_0(2000) = 2.9 \times 10^{-3}$

$$\lambda_0 = 1450 \text{ nm}$$

(Q)  $\lambda_0(3000) = 2.9 \times 10^{-3}$

$$\lambda_0 = \frac{2900}{3} \text{ nm}$$

(R)  $\lambda_0 = 580 \text{ nm}$

(S)  $\lambda_0 = 290 \text{ nm}$

$$\phi = 4 \text{ eV}$$

$$\Rightarrow \lambda_T = \frac{1240}{4} = 310 \text{ nm}$$

To emit photoelectron

$$\lambda_0 < \lambda_T$$



$\lambda_0 = 580$  lie in visible range

$\Rightarrow$  R  $\rightarrow$  2

Power  $\propto T^4$

$\Rightarrow \frac{P_1}{P_2} = \left(\frac{T_1}{T_2}\right)^4$

$\frac{1}{16} = \left(\frac{T_1}{6000}\right)^4$

$\frac{T_1}{6000} = \frac{1}{2}$

$\Rightarrow T_1 = 3000$  K

Q  $\rightarrow$  4

$\lambda$  is maximum for P.

$\sin \theta = \frac{\lambda}{d}$

$2\theta =$  width of central maximum

$\Rightarrow$  width  $\propto \lambda$ .

$\Rightarrow$  max<sup>m</sup> width of (P)

P  $\rightarrow$  3

P  $\rightarrow$  3, Q  $\rightarrow$  4, R  $\rightarrow$  2, S  $\rightarrow$  1.

16. Correct option is (B).

$\omega_0 = 10^5 \text{ rad s}^{-1}, L = 50 \times 10^{-3} \text{ H}$

$\Rightarrow X_L = 5000 \Omega = X_C$  (at resonance)

$\frac{1}{\sqrt{LC}} = \omega_0$

$\Rightarrow L_C = \frac{1}{\omega_0^2}$

$\Rightarrow C = 2 \times 10^{-9} \text{ F}$

$I_0 = \frac{\epsilon_0}{\sqrt{R^2 + (X_L - X_C)^2}}$

$I_0 = \frac{\epsilon_0}{R} \dots(1)$

$0.05I_0 = \frac{\epsilon_0}{\sqrt{R^2 + (X_L - X_C)^2}} \dots(2)$

at  $\omega = 8 \times 10^4 \text{ rad s}^{-1}$

$X_L = 8 \times 10^4 \times 50 \times 10^{-3} = 4000 \Omega$

$X_C = \frac{1}{\omega C} = 6250 \Omega$

From (1) and (2), we get

$\sqrt{R^2 + (X_L - X_C)^2} = \frac{R}{0.05}$

$R^2 + (6250 - 4000)^2 = 400R^2$

$\Rightarrow R^2 \approx \frac{(2250)^2}{400}$

$R = \frac{2250}{20} = 112.5 \Omega$

$I_0 = \frac{\epsilon_0}{R} = \frac{45}{112.5}$

$= 400 \text{ mA}$

(P  $\rightarrow$  3)

$\rightarrow Q = \frac{1}{R} \sqrt{\frac{L}{C}}$

$\Rightarrow Q = \frac{2}{2250} \times \sqrt{\frac{50 \times 10^{-3}}{2 \times 10^{-7}}} = \frac{10^4}{225}$

$= 44.4$  (Q  $\rightarrow$  1)

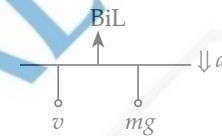
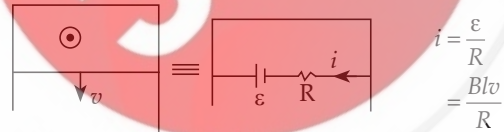
$Q = \frac{\omega_0}{BW}$

$\Rightarrow BW = \frac{\omega_0}{Q} = \frac{10^5}{\frac{10^4}{225}} = 2250$  (R  $\rightarrow$  4)

$P = \frac{\epsilon_0^2}{R}$  (peak power)

$= \frac{45^2}{112.5} = 18 \text{ W}$  (S  $\rightarrow$  2)

17. Correct option is (D).



$a = \frac{\Sigma F}{m}$

$= \frac{mg - Bil}{m}$

$= g - \frac{B^2 l^2}{mR} v = 10 - 5v$

$\frac{dv}{dt} = 10 - 5v$

$\Rightarrow \int_0^v \frac{dv}{10 - 5v} = \int_0^t dt$

$\Rightarrow v = 2(1 - e^{-5t})$

at  $t = 0.2 \text{ sec}$   $v = 1.2 \text{ m s}^{-1}$

$\epsilon = Blv$

$= 1.2V$

$F = \frac{B^2 l^2 v}{R} = 0.12 \text{ N}$

$P = \frac{B^2 l^2 v^2}{R} = 0.144 \text{ W}$

Terminal velocity,  $g = \frac{B^2 l^2 v_0}{mR}$

$v_0 = 2 \text{ ms}^{-1}$

P  $\rightarrow$  3, Q  $\rightarrow$  4, R  $\rightarrow$  2, S  $\rightarrow$  5.